1. Compare three projects: Write out your solution, by hand, in terms of Interest Factors, then with equations, then substituting values in the equations. Finally, substitute the final value of the interest factor. Of course, once this is done for a given interest factor--e.g., (P/F,0.04,5)--you can go directly from the interest factor to the final value. Use an effective annual interest rate of 4\%. You may check your answers with Excel.
2. Create cash flow tables from the information given below, 4,6 , and 12 years, respectively. Also do 12 year cash flow tables for $A$ and $B$.

| Cash Type | Project A | Project B | Project C ${ }^{\text {a }}$ |
| :---: | :---: | :---: | :---: |
| Capital Cost, \$ | 40,000 | 20,000 | 65,000 |
| Revenue, $\mathbf{\$ / y r}$ | 13,000 | 11,000 | $\mathrm{A}+\mathrm{G}(\mathrm{A}=7,000$ <br> $\mathrm{G}=2,000)$ |
| O\&M, \$/yr | 6,000 | 3,000 | 4,000 |
| Salvage Value, \$ | 9,000 | 5,000 | 4,000 |
| Lifetime, yr | 4 | 6 | 12 |

${ }^{\text {a }}$ Project C Revenue $=7,000$ first year \& increases 2,000/year thereafter (i.e., 7,000, 9,000, 11,000,...)
2. Determine the Present Worth of the three alternatives. Use 12 yr cash flow tables.
3. Determine the Annual Cash Flow of each Project. Use 6 AND 12 yr cash flow tables for Project B (just to prove that both give the same answer).
4. Determine the Rate of Return ( $i^{*}$ ) of each project, using a trial by error method. Stop when you get an $i^{*}$ value that gives a PW of $0 \pm \leq \$ 50$
5. Determine the discounted payback period for each project. Use the project lifetime cash flow table.
6. Determine the undiscounted payback period for each project. Use the project lifetime cash flow table.
7. Which project has the maximum net benefit (Present or annual)? Which has the best Return Rate? The best Payback Period? Why can the methods give different answers?

## Solution:

| 1 | End of Year | A | A* | B | B* | C |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0 | -40 | -40 | -20 | -20 | -65 |  |  |  |  |
|  | 1 | 7 | 7 | 8 | 8 | 3 |  |  |  |  |
|  | 2 | 7 | 7 | 8 | 8 | 5 |  |  |  |  |
|  | 3 | 7 | 7 | 8 | 8 | 7 |  |  |  |  |
|  | 4 | 16 | -24 | 8 | 8 | 9 |  |  |  |  |
|  | 5 |  | 7 | 8 | 8 | 11 |  |  |  |  |
|  | 6 |  | 7 | 13 | -7 | 13 |  |  |  |  |
|  | 7 |  | 7 |  | 8 | 15 |  |  |  |  |
|  | 8 |  | -24 |  | 8 | 17 |  |  |  |  |
|  | 9 |  | 7 |  | 8 | 19 |  |  |  |  |
|  | 10 |  | 7 |  | 8 | 21 |  |  |  |  |
|  | 11 |  | 7 |  | 8 | 23 |  |  |  |  |
|  | 12 |  | 16 |  | 13 | 29 |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |
| 2 | PW of CFT | NA | (\$17.83) | NA | \$46.35 | \$60.15 |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |
| 3 | ACF of PS | (\$1.90) | NA | \$4.94 | NA | \$3.37 |  |  |  |  |
|  | ACF of PV | NA | (\$1.90) | NA | \$4.94 | \$6.41 |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |
| 4 | i* of CFT | -2.7\% | -2.7\% | 34.8\% | 34.8\% | 13.5\% |  |  |  |  |
|  | PW at IRR | \$0.00 | NA | \$0.00 | \$0.00 | \$0.00 |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |
| 5 | PB Discounted | A | A PW | A Cum | B | B PW | B Cum | C | C PW | C Cum |
|  | 0 | -40 | -40 | -40 | -20 | -20 | $-20^{\prime \prime}$ | -65 | -65 | -65 |
|  | 1 | 7 | 6.7 | -33.3 | 8 | 7.7 | -12.3 | 3 | 2.9 | -62.1 |
|  | 2 | 7 | 6.5 | -26.8 | 8 | 7.4 | -4.9 | 5 | 4.6 | -57.5 |
|  | 3 | 7 | 6.2 | -20.6 | 8 | 7.1 | 2.2 | 7 | 6.2 | -51.3 |
|  | 4 | 16 | 13.7 | -6.9 | 8 | 6.8 | 9.0 | 9 | 7.7 | -43.6 |
|  | 5 |  |  |  | 8 | 6.6 | 15.6 | 11 | 9.0 | -34.5 |
|  | 6 |  |  |  | 13 | 10.3 | 25.9 | 13 | 10.3 | -24.3 |
|  | 7 |  |  |  |  |  |  | 15 | 11.4 | -12.9 |
|  | 8 |  |  |  |  |  |  | 17 | 12.4 | -0.4 |
|  | 9 |  |  |  |  |  |  | 19 | 13.3 | 12.9 |
|  | 10 |  |  |  |  |  |  | 21 | 14.2 | 27.1 |
|  | 11 |  |  |  |  |  |  | 23 | 14.9 | 42.0 |
|  | 12 |  |  |  |  |  |  | 29 | 18.1 | 60.1 |
|  |  |  |  | No PB |  |  | 3 |  |  | 9 |
|  | Year |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |
| 6 | PB Undiscounted | A | A Cum | B | B Cum | C | C Cum |  |  |  |
|  | 0 | -40 | -40 | -20 | -20 | -65 | -65 |  |  |  |
|  | 1 | 7 | -33 | 8 | -12 | 3 | -62 |  |  |  |
|  | 2 | 7 | -26 | 8 | -4 | 5 | -57 |  |  |  |
|  | 3 | 7 | -19 | 8 | 4 | 7 | -50 |  |  |  |
|  | 4 | 16 | -3 | 8 | 12 | 9 | -41 |  |  |  |
|  | 5 |  |  | 8 | 20 | 11 | -30 |  |  |  |
|  | 6 |  |  | 13 | 33 | 13 | -17 |  |  |  |
|  | 7 |  |  |  |  | 15 | -2 |  |  |  |
|  | 8 |  |  |  |  | 17 | 15 |  |  |  |
|  | 9 |  |  |  |  | 19 | 34 |  |  |  |
|  | 10 |  |  |  |  | 21 | 55 |  |  |  |
|  | 11 |  |  |  |  | 23 | 78 |  |  |  |
|  | 12 |  |  |  |  | 29 | 107 |  |  |  |

2. Compare alternative indoor lighting scenarios for your family home (NOT your dorm room). Compare incandescents (Halcos) and compact fluorescents (Energy Misers). Investigate using ALL incandescents or ALL fluorescents where ever a 40, 60, or 100W incandescent is (or could be) in use, e.g., lamps and ceiling fixtures. Do not evaluate linear florescent tubes, flood lights, etc. MARR $=0.06$. Determine answers with calculator (to prepare for the test) and Excel (to prepare for the real world). Turn in your Excel solution, appropriately documented.

Table 1: Bulb Information*

| Bulb | Wattage, W | Incandescent <br> Equivalent, W | Lifetime (in operation), hr | Price, \$ | Picture |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Halco \# 6320 | 40 | It is Incandescent! | 5,000 | 0.50 |  |
| Halco \# 6321 | 60 | It is Incandescent! | 5,000 | 0.55 | 3 |
| Halco \# 6323 | 100 | It is Incandescent! | 5,000 | 0.60 | T |
| Energy Miser FE-IISB-9W | 9 | 40 | 10,000 | 2.70 | (1) |
| Energy Miser FE-IISB-14W/41K | 14 | 60 | 10,000 | 2.80 | 15 |
| Energy Miser FE-IISB-23W/27K | 23 | 100 | 12,000 (we'll assume 10,000) | 2.90 | [1] |

*1000Bulbs.cpm (2010) "1000Bulbs.com". www.1000bulbs.com, accessed Sept. 11, 2013. Prices changed to provide new problem.

1. Import Table 1 into Excel and add the following columns: Daily Operation, hr; Lifetime (Elapsed), yr; Number of Bulbs; Total Purchase Cost, \$; Annual Electric, kWhr; Annual Electric, \$. Assume the Daily operation is $\mathbf{3 . 4 2 5}$ hours per day, 365 days per year. This will give an 8 and 4 year elapsed lifetime for the CFL \& INC light bulbs, respectively. Base the number of each bulb type on your home. First determine the number of INCs of each type you need (if ALL bulbs were INCs), and then repeat using the SAME numbers for the equivalent CFLs (if ALL bulbs were CFLs). We are looking at the economic benefit of switching from ALL INCs to ALL CFLs. Assume electricity cost = $\mathbf{\$ 0 . 1 3 / k W h r}$. Document how the table values were determined (some were "Given", others are calculated using equations). See Prof Everett's Course page and use the "Student Reference" link for guidance on "How to document tables".
2. Make an 8 yr cash flow table for the INC and CFL Alternatives. There will be one column for the CFLs and one for the INCs. The INC Alternative will be repeated twice, as you will need to replace the INC light bulbs after 4 years. While only the PW analysis requires you to double the INC Alternative, using it for the other analyses is OK as you'll get the same answer either way for them. These two cash flow tables will only have costs, i.e. the cost of purchasing bulbs and powering them. All of the values will be negative! And no Salvage Costs!
3. Add a third cash flow column to the 8 yr cash flow table that is the CFL cash flow column MINUS the INC cash flow column, i.e., subtract each year's values. This column should have a negative amount at the end of year 0 and positive amounts in all other years. The CFLs should cost more to purchase than the INCs, but should cost less to power. Estimate the PWNB and ANB of this cash flow table. These numbers give the net benefit of switching from ALL INC to ALL CFL. Also determine the rate of return and discounted payback period associated with switching from INC to CFL. You'll need two more columns to do the discounted payback period. Interpret your answers.
4. What assumptions used to complete steps 1-3 do you think are most inappropriate for your home?

If you haven't already switched to CFLs, I hope this convinces you! But make sure you dispose of CFLs properly, as they contain mercury. Do you disagree with any of the assumption I used?

You can use my solution to check your excel solution, but YOUR homework MUST have DIFFERENT numbers of bulbs. I assumed five 40W, ten 60W \& twenty 100W INCs (and the same numbers of CFLs) and ended up with (third cash flow column) PW=\$2111, ANB = \$340, $\mathrm{i}^{*}=441 \%$, Payback Period = 1 year. Outstanding i* and Payback Period! Why do people still buy incandescent bulbs? :)

## Solution:

| Table 1: Li | ght Bulb In | nformation |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Bulb | Wattage W | Equivalent to (Inc.) W | Lifetime (operation) hr | Daily <br> Operation <br> hr/d | Lifetime (elapsed) d | $\begin{array}{\|c} \hline \text { Lifetime } \\ \text { (elapsed) } \\ \mathrm{yr} \end{array}$ | Price (each) \$ | Quantity | Total Purchase Cost \$ | Annual <br> Electric kWhr | Annual <br> Electric \$ |
| (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) |
| $\begin{gathered} \text { Halco \# } \\ 6320 \end{gathered}$ | 40 | It is Incandesce $n t!$ | 5,000 | 3.425 | 1460 | 4 | 0.5 | 5 | 2.5 | 250 | \$33 |
| $\begin{gathered} \text { Halco \# } \\ 6321 \end{gathered}$ | 60 | It is Incandesce nt! | 5,000 | 3.425 | 1460 | 4 | 0.55 | 10 | 5.5 | 750 | \$98 |
| Halco \# $6323$ | 100 | It is Incandesce nt! | 5,000 | 3.425 | 1460 | 4 | 0.6 | 20 | 12 | 2500 | \$325 |
| Energy Miser FE-IIS-9W | 9 | 40 | 10,000 | 3.425 | 2920 | 8 | 2.7 | 5 | 13.5 | 56 | \$7 |
| Energy Miser FE-IISB14W/41K | 14 | 60 | 10,000 | 3.425 | 2920 | 8 | 2.8 | 10 | 28 | 175 | \$23 |
| Energy Miser FE-IIS-26W27 | 23 | 100 | 10,000 | 3.425 | 2920 | 8 | 2.9 | 20 | 58 | 575 | \$75 |
| Columns 1 | -5 \& 8 we | ere given |  |  |  |  |  | 5 | 6 | 6 | 6 |
| Column 6 | $=\mathrm{Col} 4 / \mathrm{Co}$ | ol 5 |  |  |  | Elecrtricit | ty Price | 0.13 | \$/kWhr |  |  |
| Column 7 | = Col $6 / 36$ |  |  |  |  |  | MARR | 0.06 | MARR |  |  |
| Column 9 | is assumed | d (based on lis | lights needed | d for home) |  |  |  |  |  |  |  |
| Column 10 | = Col 9x | Col 8 |  |  |  | Orig \#-5, | 10, 20 |  |  |  |  |
| Column 11 | $1=\mathrm{Col} 2 \times$ | Col $5 \times \mathrm{Col} 9 \times$ | x 365/1000 |  |  |  |  |  |  |  |  |
| Column 12 | = Col 11 x | Electricity P | Price |  |  |  |  |  |  |  |  |
|  | 5 | 5 | 5 |  |  |  |  |  |  |  |  |
| Table 2: Ca | ash Flow Ta | ables |  |  |  |  |  |  |  |  |  |
| End of yr | CFL \$ | INC \$ | CFL-INC \$ | PW \$ | Cum-PW \$ |  |  |  |  |  |  |
| (1) | (2) | (3) | (4) | (5) | (6) | Answers | CFL | INC | CFL-INC |  |  |
| 0 | -99.5 | -20 | -80 | -80 | -80 | PWNB | -\$750 | -\$2,862 | \$2,111 |  | 10 |
| 1 | -\$105 | -\$455 | 350 | 330 | 251 | ANB | -\$121 | -\$461 | \$340 |  |  |
| 2 | -\$105 | -\$455 | 350 | 312 | 563 |  |  |  |  |  |  |
| 3 | -\$105 | -\$455 | 350 | 294 | 857 | RR |  |  | 441\% |  | 10 |
| 4 | -\$105 | -\$475 | 370 | 293 | 1150 | B-C Ratio |  |  | 27.56 |  | 10 |
| 5 | -\$105 | -\$455 | 350 | 262 | 1412 | PayBack Peric | eriod |  |  | yr | 10 |
| 6 | -\$105 | -\$455 | 350 | 247 | 1658 |  |  |  |  |  |  |
| 7 | -\$105 | -\$455 | 350 | 233 | 1891 |  |  |  |  | No Doc |  |
| 8 | -\$105 | -\$455 | 350 | 220 | 2111 |  |  |  |  |  |  |

Column 1 is given
Column 2 is the cost to purchase CFLs (yr 0) and to power (yrs 1-8), From Table 1
Column 3 is the cost to purchase INCs (yr $0 \& 4$ ) and to power (yrs 1-8), From Table 1
Column 4 = Col 2 - Col 1

Column $5=$ Present worth of $\mathrm{Col} 4=\mathrm{Col} 4 \times(1+\mathrm{MARR})^{\wedge} \mathrm{Col} 1$
Column 6 is the cumulative sum of Col 5

## Selected Sample Calculations

PW_CFL = -PC_CFL - AEC_CFL x (P/A, i,8)
PW_INC = -PC_INC - AEC_INC x (P/A,i,8) - PC_INC x (P/F,i,4)
ANB_CFL = -PC_CFL x (A/P, i,8) - AEC_CFL
ANB_INC=-PC_INC x (A/P,i,8) - AEC_INC - PC_INC x (P/F,i, 4 )(A/P, $\mathrm{i}, 8)$
RR - Solve the following equation for i*: AES x (P/A,i8,8) - (PC_CFL - PC_INC) + PC_INC x (P/F,i8,4) = 0

